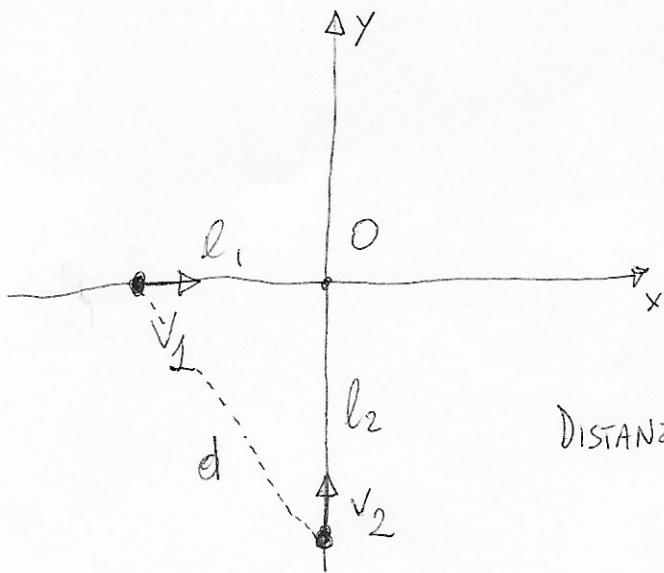


②



$$\textcircled{1} \quad \begin{aligned} x &= -l_1 + v_1 t \\ y &= 0 \end{aligned}$$

$$\textcircled{2} \quad \begin{aligned} x &= 0 \\ y &= -l_2 + v_2 t \end{aligned}$$

DISTANZA $d = \sqrt{(-l_1 + v_1 t)^2 + (-l_2 + v_2 t)^2}$

DISTANZA MINIMA $\frac{\partial d}{\partial t} = 0$

$$\frac{\partial d}{\partial t} = \frac{2v_1(-l_1 + v_1 t) + 2v_2(-l_2 + v_2 t)}{2\sqrt{(-l_1 + v_1 t)^2 + (-l_2 + v_2 t)^2}} = 0$$

$$-l_1 v_1 + v_1^2 t - l_2 v_2 + v_2^2 t = 0$$

$$t = \frac{l_1 v_1 + l_2 v_2}{v_1^2 + v_2^2}$$

$$d_{\text{MIN}} = \sqrt{\left(-l_1 + v_1 \frac{l_1 v_1 + l_2 v_2}{v_1^2 + v_2^2}\right)^2 + \left(-l_2 + v_2 \frac{l_1 v_1 + l_2 v_2}{v_1^2 + v_2^2}\right)^2} =$$

$$= \sqrt{\frac{(-l_1 v_1^2 - l_1 v_2^2 + v_1^2 l_1 + v_1 v_2 l_2)^2 + (-l_2 v_1^2 - l_2 v_2^2 + l_1 v_2 v_1 + l_2 v_2^2)^2}{(v_1^2 + v_2^2)^2}} =$$

$$= \sqrt{\frac{l_1^2 v_1^4 + v_1^2 v_2^2 l_2^2 - 2 l_1 l_2 v_1 v_2^3 + l_2^2 v_1^4 + l_1^2 v_1 v_2^2 - 2 l_1 l_2 v_1^3 v_2}{(v_1^2 + v_2^2)^2}} =$$

$$= \frac{(v_1^2 + v_2^2)(l_1 v_2^2 + v_1^2 l_2^2 - 2 v_1 v_2 l_1 l_2)}{(v_1^2 + v_2^2)^2} = \frac{|l_1 v_2 - l_2 v_1|}{\sqrt{v_1^2 + v_2^2}}$$